

# Dynamically generated baryons states

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In principle, all the hadron states are dynamically generated in QCD.  
Discuss dynamically generated states in terms of hadronic degrees of freedom.

chiral unitary approach  
origin (interpretation) of resonance pole  
form factor of baryon resonance  
hadronic molecular states (kaonic few-body system)



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Newport News, Virginia USA*



5.17-20, 2011

# What are effective constituents in baryon resonance ??

- quarks and gluons are fundamental constituents of hadrons

but, current quarks are not effective constituents to understand hadron structure

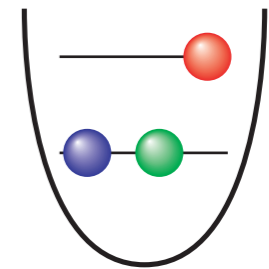
## Effective constituents in hadron

**constituent quarks** confined in a single potential

in this picture, symmetry of quarks is realized in baryon spectra through constituent quarks

ex. p-state excitation of quark for baryon resonances

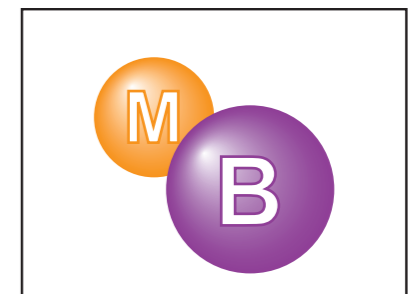
chiral partners: N(1535) chiral partner of nucleon ??



**hadrons** interacting inter-hadron force

decaying resonance  $\rightarrow$  large hadronic components

inter-hadron dynamics is important



**mixture of them**

quark source + hadron cloud

# Dynamical description of resonance

take chiral unitary model as an example: most of dynamical descriptions are based on the same concept but with different ingredients  
calculate scattering amplitude, in which resonances are expressed as poles in complex energy plane

Lippmann-Schwinger eq.

$$T = V + VGT$$

## ingredients

G: loop function (model space)

guarantee **unitarity**

V: kernel potential (dynamics)

given by **chiral Lagrangian**

If these ingredients are written in terms of hadrons, the scattering amplitude is described by hadron dynamics.

## dynamically generated state

state obtained without explicit pole terms in kernel potential V

explicit pole term represents state outside of model space (quark-origin state)

**dynamically generated state = hadronic composite state ??**

here we will see not all the states described in this way are hadronic composites

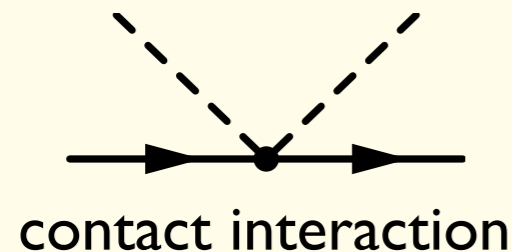
# Chiral unitary approach

## **V: kernel potential (dynamics)** a la **Chiral Perturbation Theory**

in s-wave

interactions are well organized in terms of momentum expansion

### - leading term (WT term)



coming from t-channel vector meson exchange

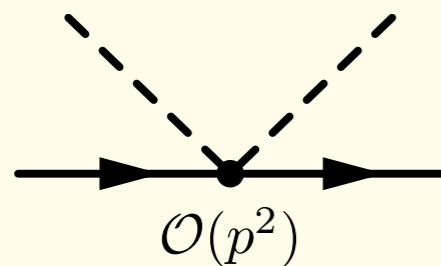
→ **no source for s-channel baryon resonances**

### - higher order terms

in these terms dynamics beyond hadronic description can be hidden



**explicit s-channel resonance contributions**



**contact terms** also can have source of resonances

ex.  $\Delta$  in higher order of  $\pi N$  chiral lagrangian

Once we use these interactions, the hidden resonances can be **reconstructed**.

For interactions derived not from chiral effective theory, it is hard to interpret their origins.

This kind of discussion is important for the interpretation of the resonance structure, but in the description of resonance how to construct the resonance is not an issue.

# Chiral unitary approach

$$T = V + VGT$$

it is necessary to regularize the loop function

## **G: loop function (model space)**

meson baryon loop function (regularization) once-subtracted dispersion relation

$$G(s) = -a(s_0) - \frac{1}{2\pi} \int_{s_+}^{\infty} ds' \left( \frac{\rho(s')}{s' - s - i\epsilon} - \frac{\rho(s')}{s' - s_0} \right), \quad \text{two-body phase space } \rho(s)$$

**regularization → renormalization constant**

free parameters to be fitted by experiments

in the regularization procedure, one fixes high-momentum behavior which is not controlled in the present model space. This means that some contributions coming from outside of the model space can be hidden in the regularization parameters.

( In cut-off scheme the situation is same. Form factors can have information off model space.)

Here we show that the hidden contribution can be excluded from formulation by theoretical requirement on the renormalization constant.

(natural renormalization scheme)

# Natural renormalization scheme

Hyodo, Jido, Hosaka, PRC78, 025203 ('08)

Let us propose a suitable renormalization condition for meson-baryon picture

## "natural" renormalization condition

### 1) consistency with meson-baryon picture

there are no states below the threshold

$$G(W) \leq 0 \quad W \leq M + m$$

### 2) consistency with chiral (loop) expansion

$$T(W) = V(W) \quad \text{at some point in} \quad M \leq W \leq M + m$$

$$G(W) = 0$$

$$G(W) \sim \sum_n \frac{1}{W - E_n}$$

satisfied automatically by 3  
dim. cutoff regularization

$$T = V + VGT$$

since the loop function is a decreasing function in terms of energy below the threshold, these two conditions can be satisfied by

$$G(M; a_{\text{natural}}) = 0$$

proposed in different contexts by Igi-Hikasa and Lutz-Kolomeitsev  
natural size of  $a$  obtained in 3 dim. cutoff with 630 MeV

# Interpretation of pole

Hyodo, Jido, Hosaka, PRC78, 025203 ('08)

no source of state originated by quarks (out of model space)

if we use **WT interaction** in  $V$  and take **natural renormalization** scheme in  $G$

$$T(W) = \frac{1}{V_{WT}^{-1}(W) - G(W; a)}$$

compare consequences from two different renormalization schemes

## chiral unitary model

model parameters tuned so as to

a) reproduce scattering data

▲ **Pheno.**

b) exclude quark-origin states theoretically

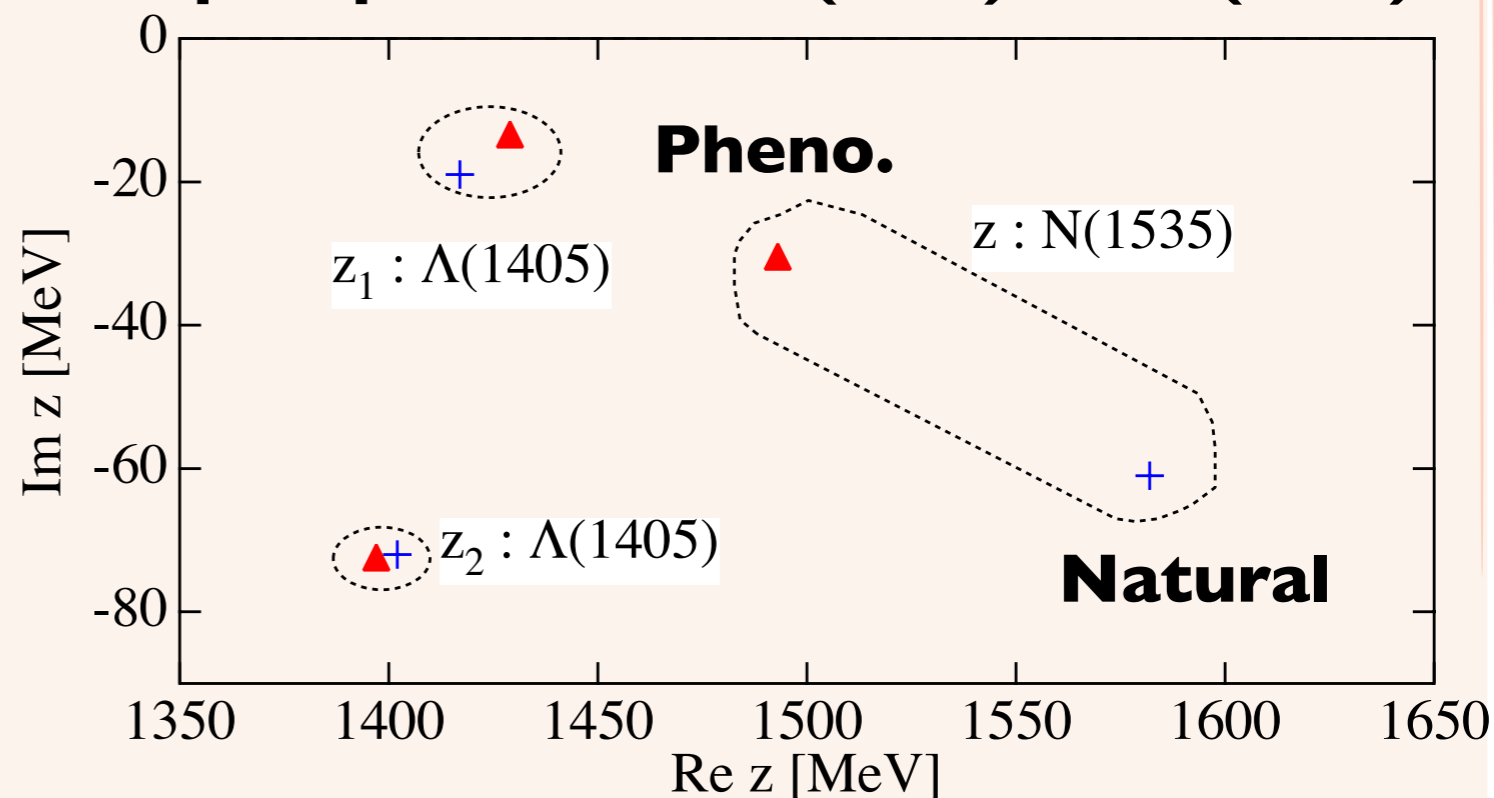
+ **Natural**

**V : WT term**

**$\Lambda(1405)$  has mostly meson-baryon components.**

**$N(1535)$  needs some other components than meson-baryon.**

## pole positions of $N(1535)$ and $\Lambda(1405)$



# Interpretation of pole

Hyodo, Jido, Hosaka, PRC78, 025203 ('08)

in natural regularization with WT interaction,

$\Lambda(1405)$  successfully reproduced,  $N(1535)$  not so satisfactorily

it is interesting to see which kind of interaction is necessary to reproduce phenomenological description in the natural renormalization.

**phenomenological renormalization condition**

$$T(W) = \frac{1}{V_{WT}^{-1}(W) - G(W; a_{\text{pheno.}})} \quad V_{WT}(W) = -\frac{C}{2f^2}(W - M)$$

**natural renormalization condition**

$$T(W) = \frac{1}{V^{-1}(W; a_{\text{natural}}) - G(W; a_{\text{natural}})}$$

Finally the interaction kernel in the natural renormalization condition can be expressed as the WT term and a pole term.

$$V(W; a_{\text{natural}}) = \underbrace{V_{WT}(W)}_{\text{WT term}} + \underbrace{\frac{C}{2f^2} \frac{(W - M)^2}{W - M_{\text{eff.}}}}_{\text{pole term}} \quad M_{\text{eff.}} \equiv M - \frac{2f^2}{C\Delta a}$$



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## phenomenological renormalization condition

**pole mass in effective int.**

$$M_{\text{eff.}}^{\Lambda^*} \simeq 7.9 [\text{GeV}]$$

$$M_{\text{eff.}}^{N^*} = 1693 \pm 37i [\text{MeV}]$$

**quark model state ? chiral partner of N ??**

Do not take the values seriously, because these values strongly depend on the details of model parameters.

$$V^{-1}(W; a_{\text{natural}}) = G(W; a_{\text{natural}}) \quad G^{-1}(W; a_{\text{natural}}) = V(W; a_{\text{natural}})$$

Finally the interaction kernel in the natural renormalization condition can be expressed as the WT term and a pole term.

$$V(W; a_{\text{natural}}) = \underbrace{V_{WT}(W)}_{\text{WT term}} + \underbrace{\frac{C}{2f^2} \frac{(W - M)^2}{W - M_{\text{eff.}}}}_{\text{pole term}} \quad M_{\text{eff.}} \equiv M - \frac{2f^2}{C\Delta a}$$

# Applications of dynamical description

although coupled channel approach can contain some components other than meson and baryon, this is a good description of resonances in terms of hadrons.

with this description, we can calculate properties of baryon resonances:

**magnetic moments of  $\Lambda(1405)$**  DJ, Hosaka, Nacher, Oset, Ramos RPC66, 025203 (02)

**radiative decay of  $\Lambda(1405)$**  Geng, Oset, Doring, EPJA32, 201 (07)

**helicity amplitude of  $N(1535)$**  DJ, Doring, Oset, PRC77, 065207 (08)

**electromagnetic mean squared radii of  $\Lambda(1405)$**  Sekihara, Hyodo, DJ, PLB669, 133 (08)

**helicity amplitudes of  $\Lambda(1670)$  and  $\Lambda(1405)$**  Doring, DJ, Oset EPJA45, 319 (10)

**electromagnetic form factors of  $\Lambda(1405)$**  Sekihara, Hyodo, DJ, PRC83, 055202(11)

## many applications for reaction calculations

coupled channel approach

describes both resonance and nonresonant scattering states

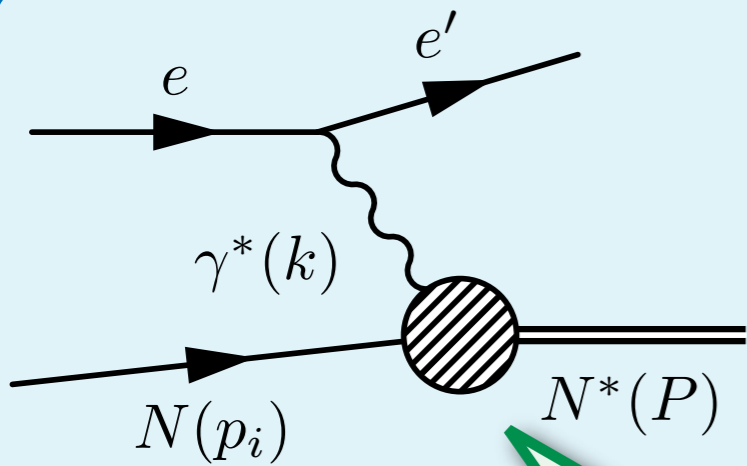
available for direct comparison with experimental data

# Transition amplitude in chiral unitary model

Jido, Döring, Oset, PRC77, 065207 (08)

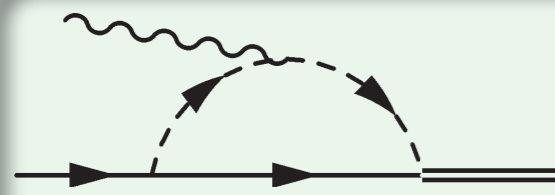
## Idea

- take chiral unitary model for  $N(1535)$  structure
- external current couples via meson and baryon

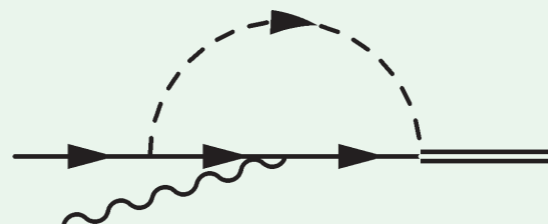


## relevant diagrams of one loop

Gauge invariant assures cancellation of divergence



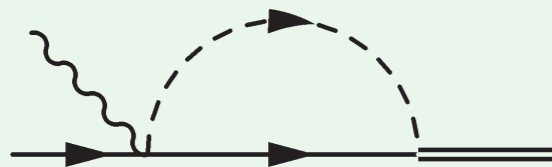
meson pole term



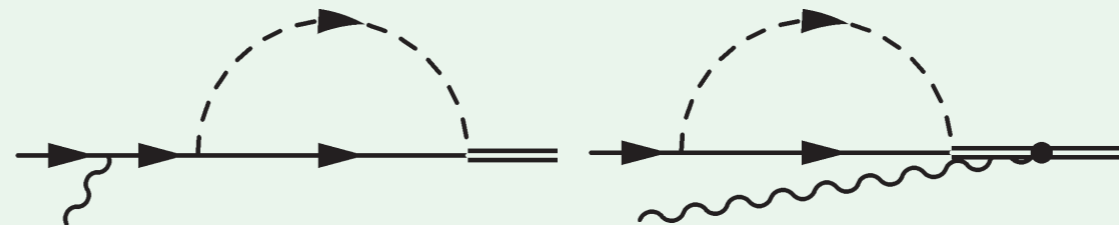
baryon pole term

$1/M$

**Z-diagram**



Kroll-Ruderman term

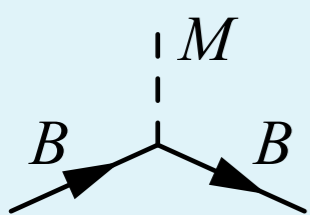


necessary for gauge invariance

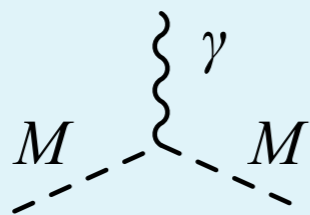
# Transition amplitude in chiral unitary model

## elementary vertices

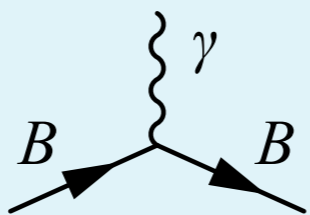
chiral Lagrangian



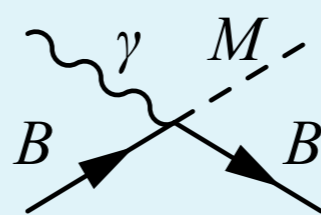
meson-baryon



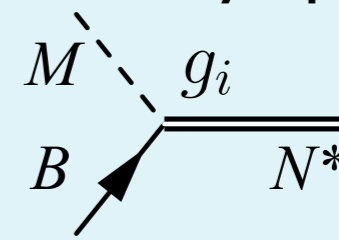
photon-meson



photon-baryon



Kroll-Ruderman

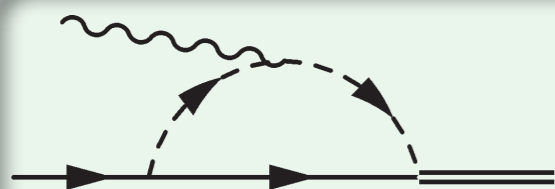


residue of pole

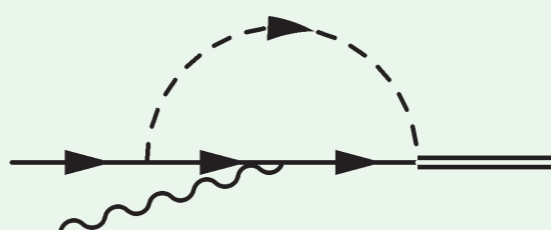
$g_i$  characterizes structure of  $N^*$

chiral unitary approach

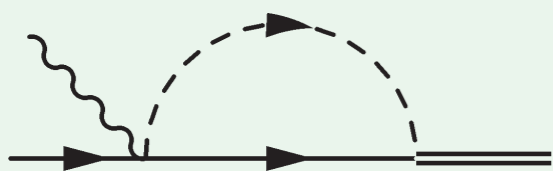
## relevant diagrams of one loop



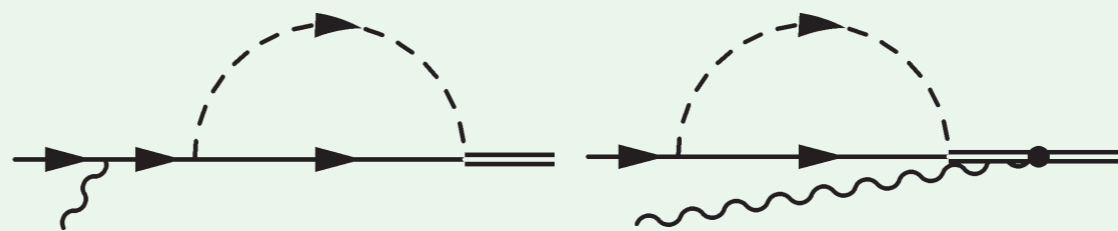
meson pole term



baryon pole term



Kroll-Ruderman term



necessary for gauge invariance

Gauge invariant assures cancellation of divergence

$1/M$

Z-diagram

# Result $A_{1/2}$ amplitude for $p^*$

Jido, Döring, Oset, PRC77, 065207 (08)

Non-relativistic calculation

## Experimental extraction

$$A_{1/2}(Q^2) = \sqrt{\frac{W\Gamma_{N^*}}{2m_p b_\eta} \sigma(W, Q^2)}$$

$\sigma$ : total cross section of  $\gamma p \rightarrow \eta p$

$$T \sim \langle \eta N | H_\eta | N^* \rangle \langle N^* | H_\gamma | \gamma N \rangle$$

photo-transition

$\Gamma_{N^*}$   **$N^*$  total width**

Data 150 MeV

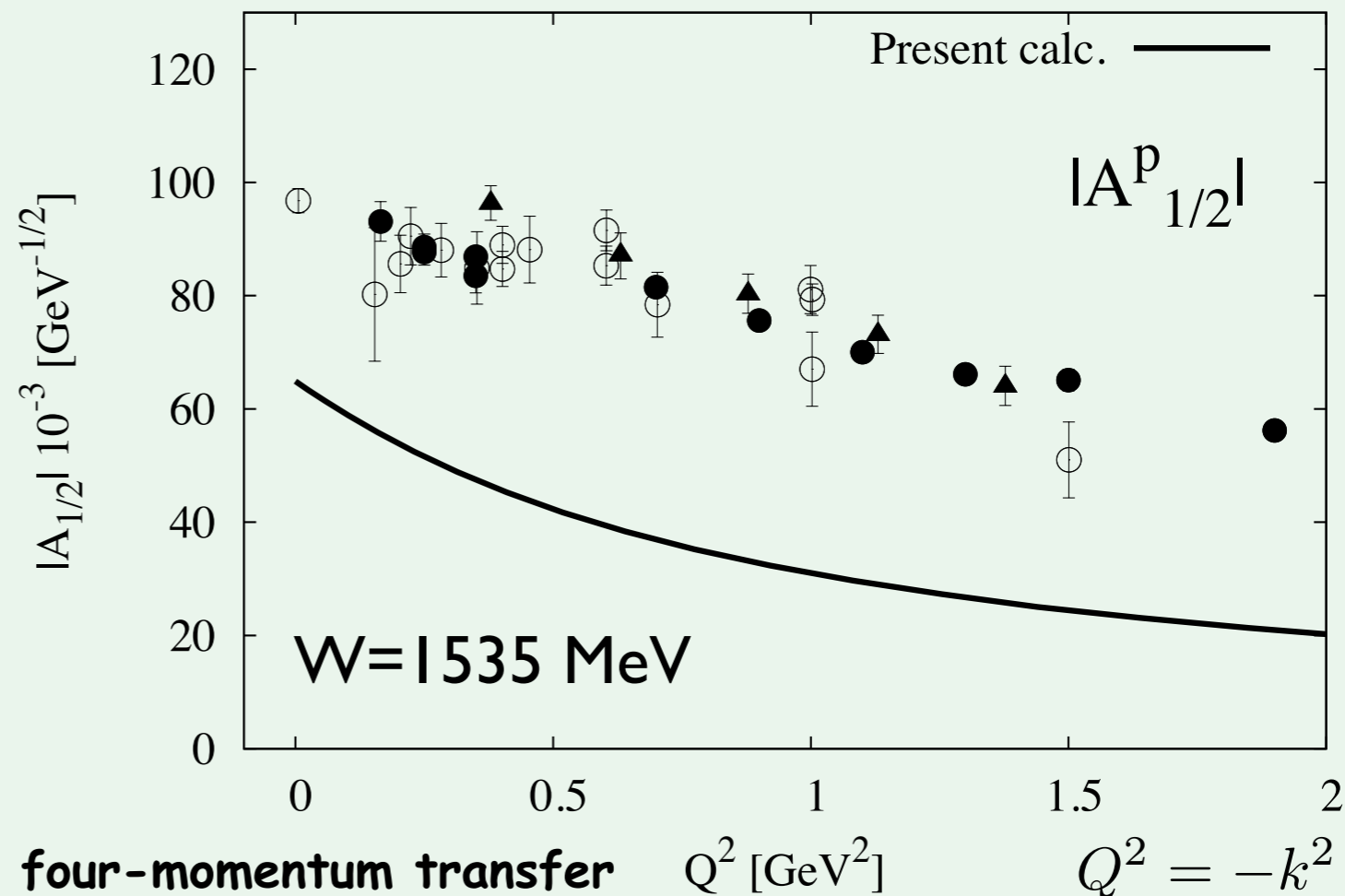
ChUM 74 MeV

$b_\eta$  **branching ratio**

Data 55%

ChUM 70%

**factor 1.6 larger**



### Experimental data

**B. Krusche et al., Phys. Rev. Lett. 74 (1995) 3736.**

H. Denizli et al. [CLAS Collaboration], Phys. Rev. C76, 015204 (2007)

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F.W. Brasse et al., Nucl. Phys. B 139, 37 (1978); Z. Phys. C22, 33 (1984).

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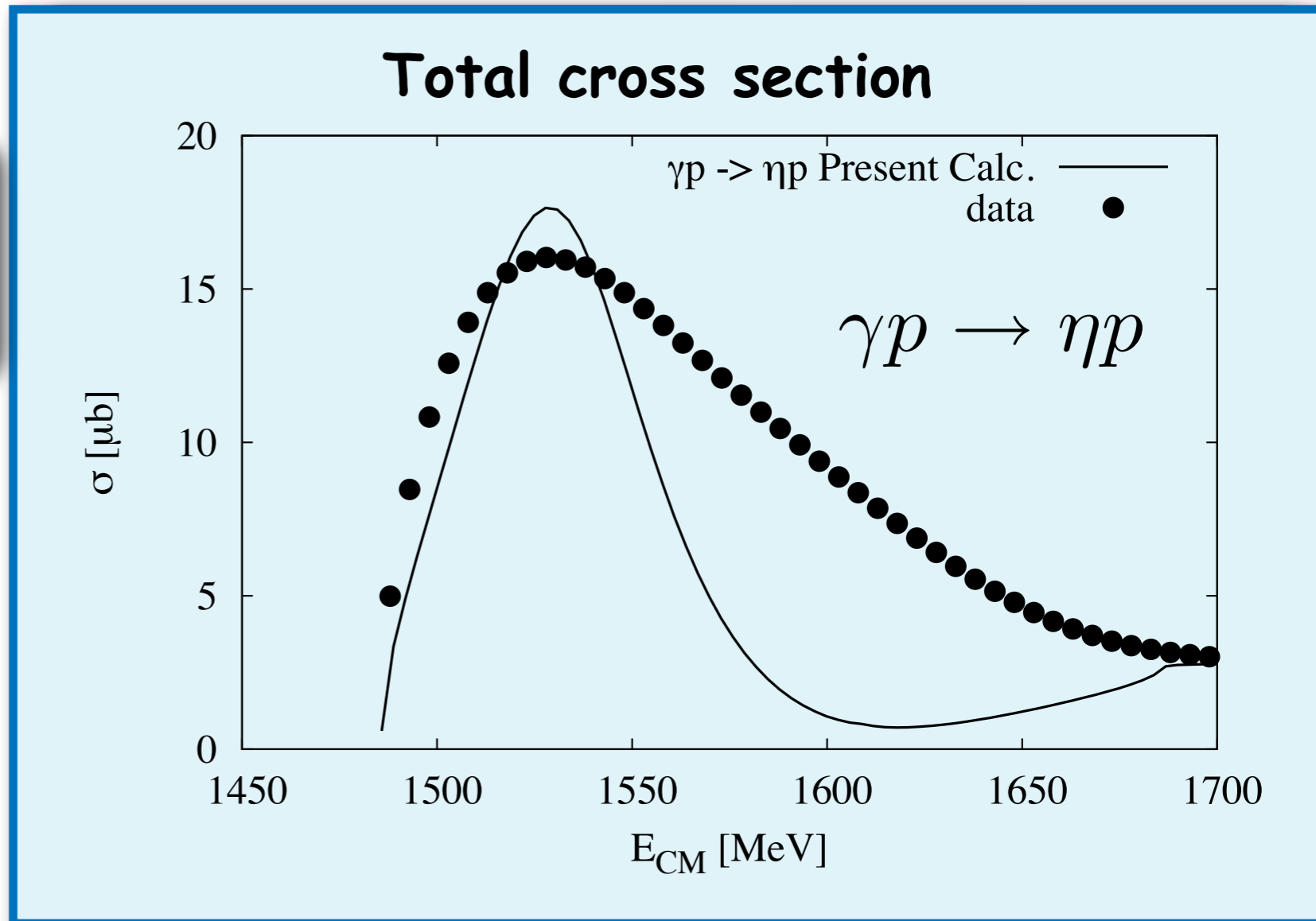
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# Further results

	our model	PDG
Values of $A_{1/2}$ at $Q^2=0$ [ $10^{-3} \text{ GeV}^{-1/2}$ ]		
$p^*$	64.88	$90 \pm 30$
$n^*$	$-51.54 + 7.2i$	$-46 \pm 27$

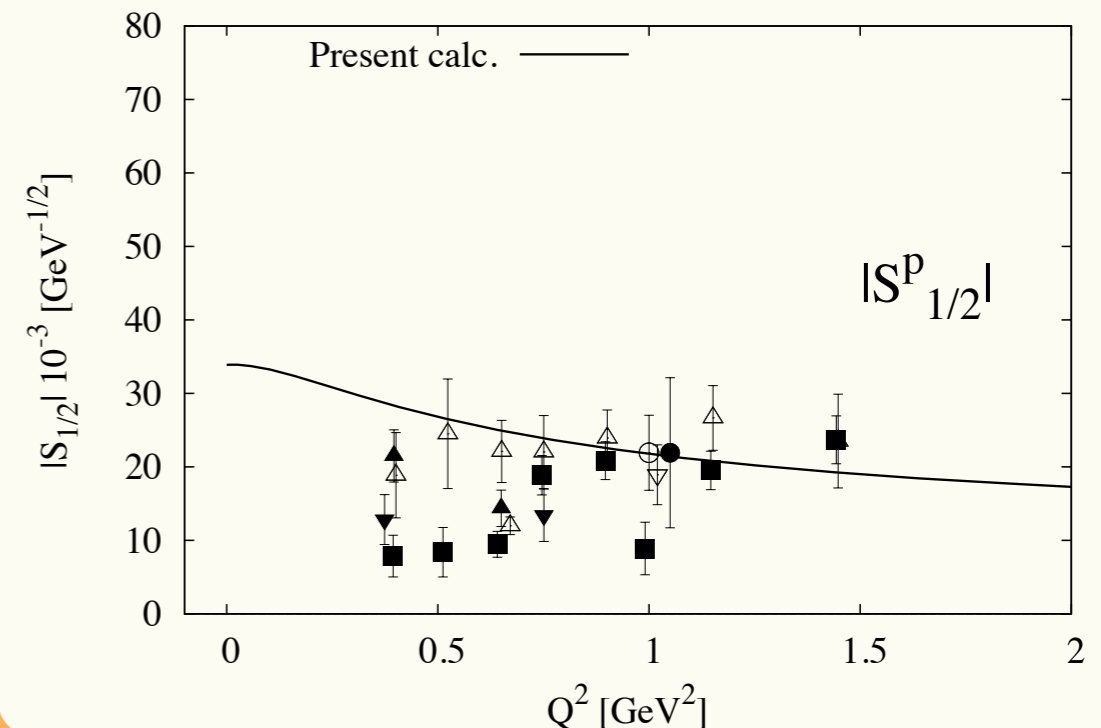
**need to fix normalization**

	our model	Exp.
Ratios of $A_{1/2}$		
$n^*/p^*$	$-0.79 + 0.1i$	$-0.84 \pm 0.15$
modulus	0.80	$0.819 \pm 0.018$
$IV/IS$	$8.94 - 1.06i$	
modulus	9.00	$10.0 \pm 0.7$

**free from norm. problem**

**isovector dominance**

$S_{1/2}$  amplitude for  $p^*$   
 negative phase respect to  $A_{1/2}$   
 consistent with data



# What we learn

- Transition form factors of  $N^*$  calculated in meson-baryon picture are consistent with data

$A_{1/2}$  and  $S_{1/2}$  for  $p^*$

n/p ratio of  $A_{1/2}$  at  $Q^2=0$

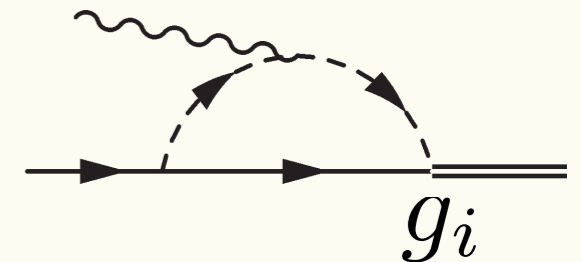
sign and magnitude

total cross section of  $\gamma p \rightarrow \eta p$

normalization problem of helicity amplitudes

need to determine  $N^*$  parameters precisely

$N(1535)$  structure : chiral unitary model  $g_i$   
meson cloud picture for photon couplings



- meson-baryon component in  $N(1535)$

sources of resonances in regularization constant

no coupling of photon to quarks

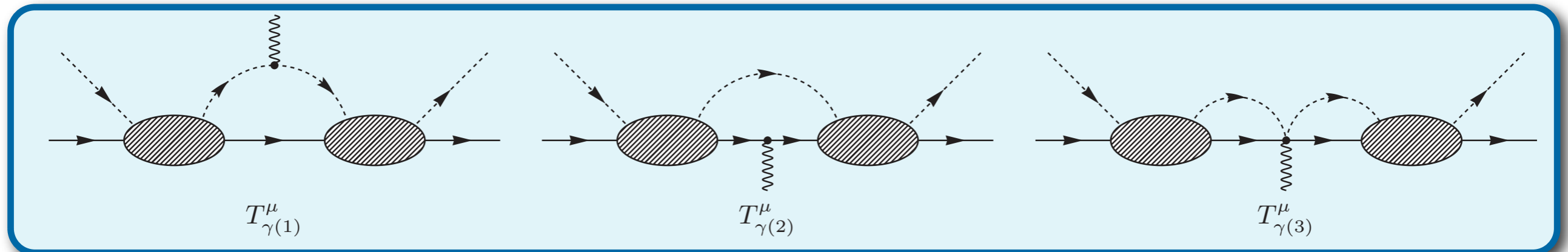
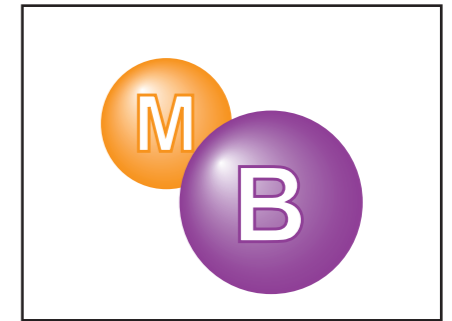
quark component less important in helicity amplitude in low  $Q^2$



# Form factors of $\Lambda(1405)$

Sekihara, Hyodo, DJ, PLB669, 133 (2008);  
PRC83, 055202 (2011)

$\Lambda(1405)$ : quasibound state of  $K^{\text{bar}}N$  with 10~30 MeV  
theoretical calculation (chiral unitary model)



# Form factors of $\Lambda(1405)$

Sekihara, Hyodo, DJ, PLB669, 133 (2008);  
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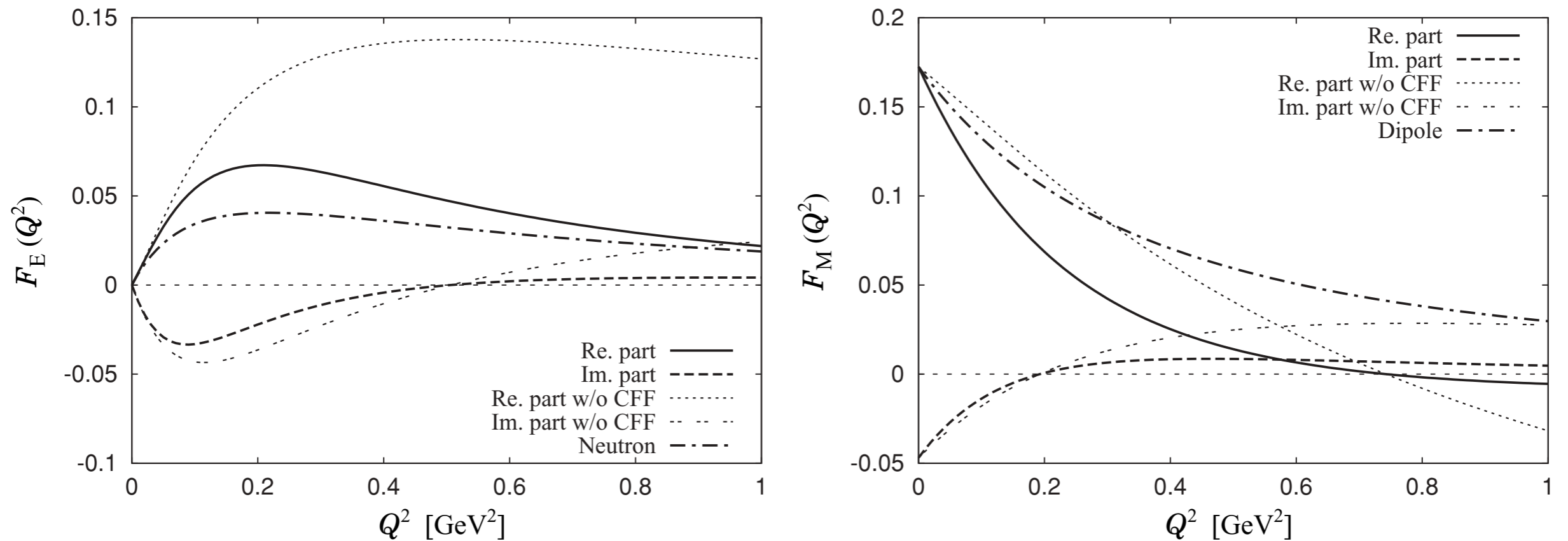
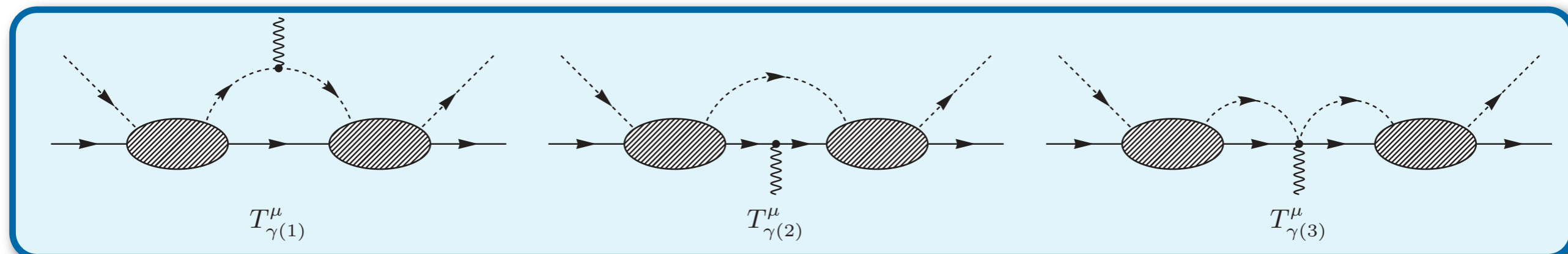
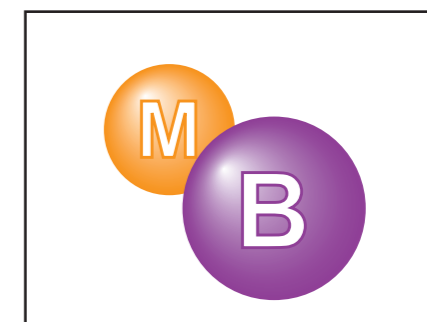


FIG. 5. Electromagnetic form factors of the  $\Lambda(1405)$  state on the higher pole position  $Z_2$ , together with the empirical form factors of the neutron. Left (right) panel shows the electric (magnetic) form factor  $F_E$  ( $F_M$ ). The label “w/o CFF” represents the result without inclusion of the common form factor in Eq. (59). The parameter  $c$  in the dipole form factor is chosen to be  $c = \text{Re}[F_M(Q^2 = 0)]$ , the real part of the magnetic moment of the  $\Lambda(1405)$ .

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theoretical calculation (chiral unitary model)



## Electromagnetic radii

$$\langle r^2 \rangle_E = -0.13 + 0.30i \quad [\text{fm}^2]$$

complex number

$$\text{moduls} \quad |\langle r^2 \rangle_E| = 0.33 \quad [\text{fm}^2]$$

$$\text{remove decay chan.} \quad \langle r^2 \rangle_E = -0.52 \quad [\text{fm}^2]$$

**spatially  
extended**

almost real Kaon surrounding nucleon  
larger radius than **neutron charge radius**

**negative  
charge radius**

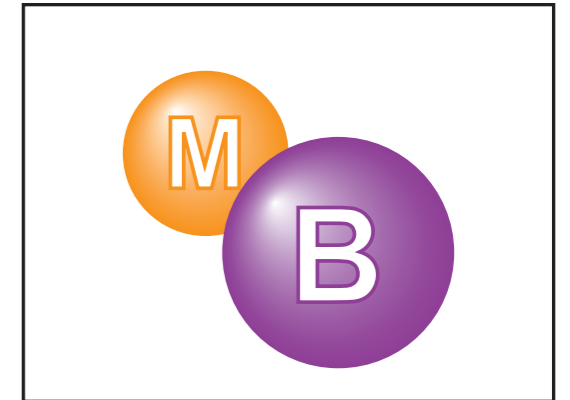
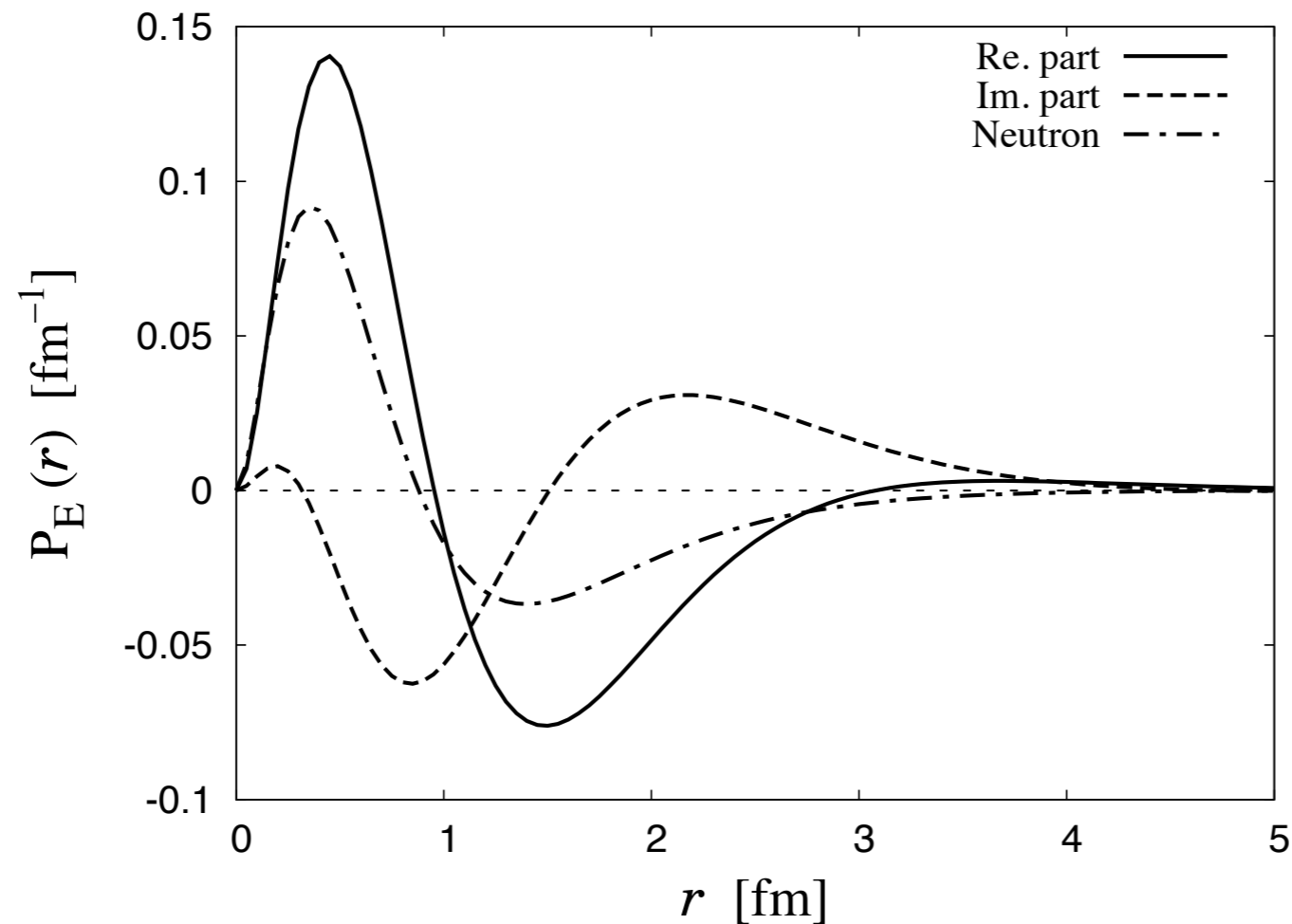
$K^-$  spreads widely around proton

$$\langle r^2 \rangle_E = -0.12 \quad [\text{fm}^2] \quad \text{virtual pion cloud}$$

# Form factors of $\Lambda(1405)$

Sekihara, Hyodo, DJ, PLB669, 133 (2008);  
PRC83, 055202 (2011)

## Electric charge distribution



**negative  
charge radius**

$K^-$  spreads widely around proton

# Hadronic molecular states

✓ composite vs elementary ?? they are mixed. Let us consider one extreme side.

## Hadronic molecular state

hadrons are constituents (nesting-box structure, Verschachtelung)

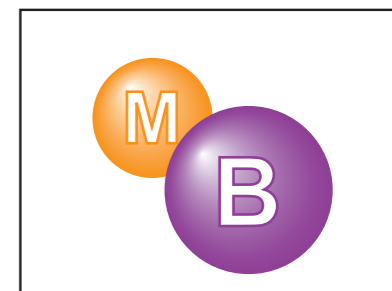
governed by hadron dynamics, not inter-quark dynamics (confinement force)

inter-hadron distance  $>$  confinement size

**larger than typical size of hadron**

ex) nucleus : bound state of baryons

deuteron,  $^3\text{He}$ , triton (NNN), hypertriton ( $\Lambda\text{pn}$ )



## Meson constituents

**resonance with decay width (quasibound state)**

transition to lighter mesons (pion)

absorptive decay modes, no meson number conservation

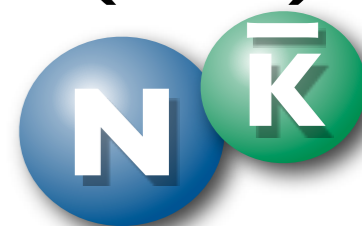
**real particles are constituents**

different from virtual pion cloud

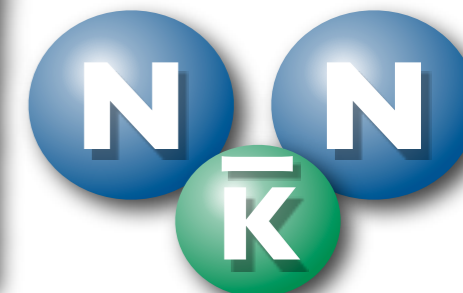
physics of threshold



$\Lambda(1405)$



$\text{K}^{\text{bar}}\text{NN}$



# size of bound state

hadronic molecular states can be realized in limited situation.

for short range interaction

**asymptotic wavefunction**

$$\psi(x) = (\text{const.}) \times \frac{\exp(-\sqrt{2\mu B_E}x)}{x}$$

$\mu$ : reduced mass  
 $B_E$ : binding energy

relative distance

$$\langle x^2 \rangle = \frac{1}{4\mu B_E}$$

for bound state with 30 MeV B.E

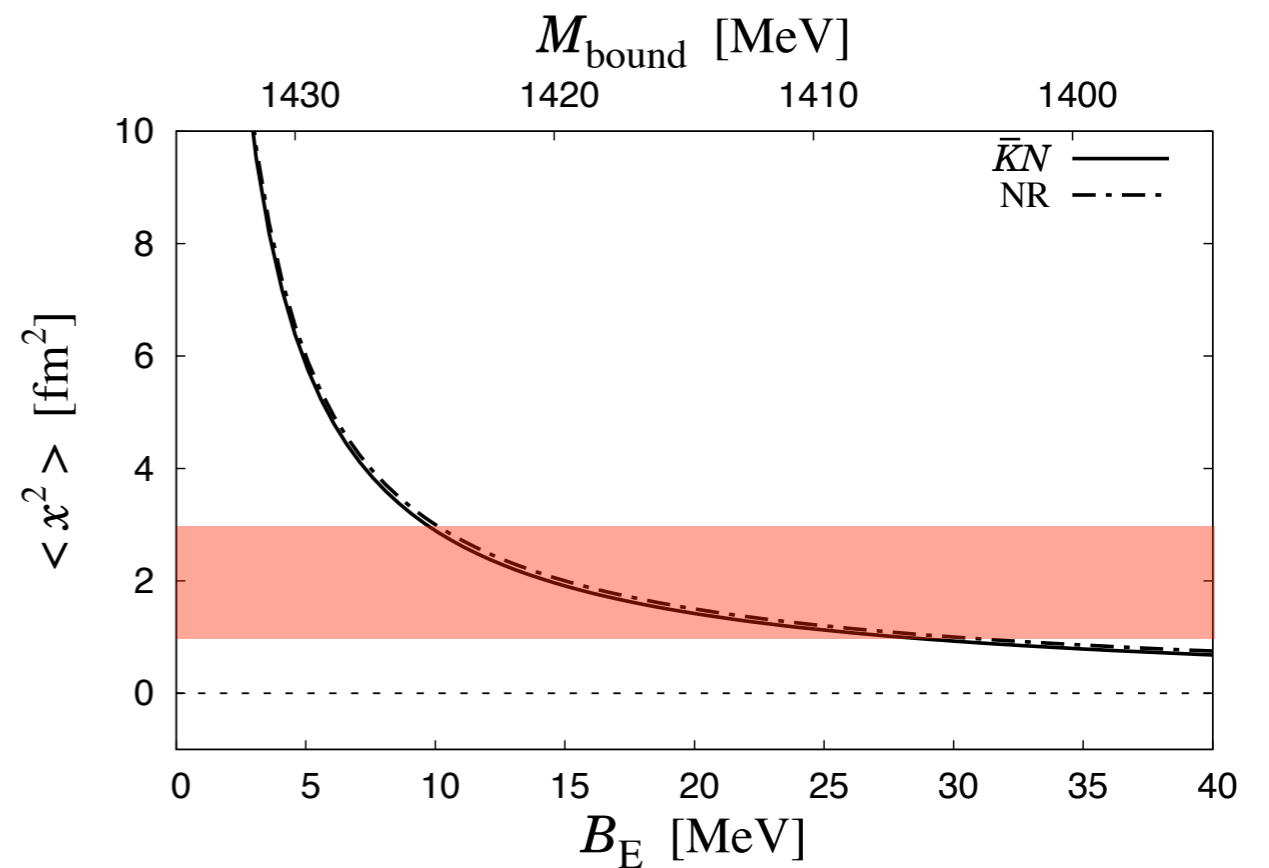
**$\bar{K}N$  system ~ 1 fm size**

typical hadron size ~ 1 fm

for deeper bound states

two hadron are overlapped  
quark dynamics should be relevant

picture of hadronic molecular is broken down



**$\bar{K}N$  system**

# Peculiarities of K meson

Y. Kanada-En'yo, DJ, PRC78, 025212 (2008)  
DJ, Y. Kanada-En'yo, PRC78, 035203 (2008)

pion is too light to be bound in range of strong interaction

kaon has moderate mass and interaction strength

## - Nambu-Goldstone boson

smaller mass compared with typical hadron mass scale

**chiral effective theory** can be applied

strong s-wave attraction in  $K^{\text{bar}}N$  and  $K^{\text{bar}}K \Rightarrow$  two-body quasibound states

## - heavy particle

half of nucleon mass

**small kinetic energy** in bound systems (BE  $\sim$  10-30 MeV)

non-relativistic potential model with decay channels

isospin averaged mass

$$m_K = 495.7 \text{ MeV}$$

$$m_N = 938.9 \text{ MeV}$$

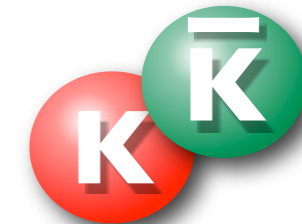
**Kaons are different from pions** in the energies of our interest !!

$\Lambda(1405)$



B.E.  $\sim$  10 to 30 MeV

$f_0(980), a_0(980)$



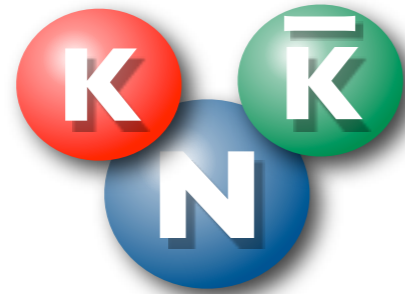
B.E.  $\sim$  10 MeV

# $K\bar{K}N$ system with $I=1/2, J^P=1/2^+$

DJ, Y. Kanada-En'yo, PRC78, 035203 (2008)

A prediction of  $KK^{\text{bar}}N$  quasibound state as an  $N^*$  resonance

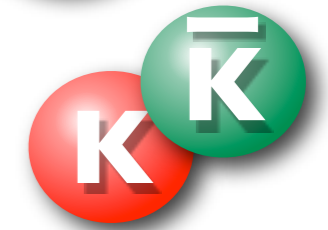
$N^*$   
 $J^P=1/2^+$



$\Lambda(1405)$



$f_0(980), a_0(980)$



## Interactions in $KK^{\text{bar}}N$ system

	$I=0$	$I=1$	threshold	open channels
$\bar{K}N$	attraction $\Lambda(1405)$	weak attraction	1434.6 MeV	$\pi\Sigma, \pi\Lambda$
$K\bar{K}$	$f_0(980)$	$a_0(980)$	991.4 MeV	$\pi\pi, \pi\eta$
$KN$	repulsion very weak	strong repulsion	1434.6 MeV	no

if 3-body BS  $\ll$  2-body BS + hadron    molecular picture broken down



# Theoretical studies of $KK^{\text{bar}}N$ system

fix two-body interaction  $\rightarrow$  calculate three-body system

$N^*$

$J^P = 1/2^+$



## 1) non-relativistic potential model

DJ, Y. Kanada-En'yo, **PRC78**, 035203 (2008)

$KK^{\text{bar}}N$  single channel

two-body interaction

$K^{\text{bar}}N$   $\Lambda(1405)$  as a quasibound state

$K^{\text{bar}}K$   $f_0(980)$  and  $a_0(980)$  as quasibound states

$KN$  adjust repulsive scattering length

## 2) relativistic Faddeev approach

Martinez Torres, Khemchandani, Oset, **PRC79**, 065207 (2009)

Martinez Torres, DJ, **PRC82**, 038202 (2010)

coupled channels,  $KK^{\text{bar}}N$ ,  $K\pi\Sigma$ ,  $K\pi\Lambda$

two-body subsystem

scattering amplitudes obtained by chiral unitary model in full coupled-channels

**meson-baryon** dynamically generated  $\Lambda(1405)$

**meson-meson** dynamically generated  $f_0(980)$  and  $a_0(980)$

non-resonant background

# Results of $KK^{\text{bar}}N$ system $N^*$ at 1910 MeV

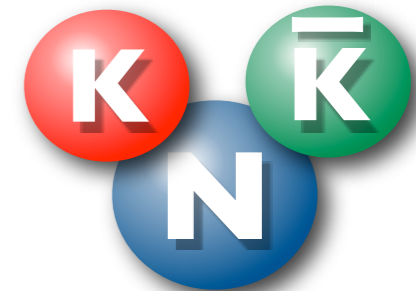
- loosely bound system threshold of  $KK^{\text{bar}}N$  1930 MeV

## 1) non-relativistic potential model

DJ, Y. Kanada-En'yo, **PRC78**, 035203 (2008)

B.E. from $KK^{\text{bar}}N$	width	mass
HW: <b>19 MeV</b>	<b>88 MeV</b>	<b>1911 MeV</b>
AY: <b>39 MeV</b>	<b>98 MeV</b>	<b>1891 MeV</b>

$N^*$



## 2) relativistic Faddeev approach

read peak position and width

$(K\bar{K}N, K\pi\Sigma, K\pi\Lambda)$

**mass: 1922 MeV, width  $\sim$ 25 MeV**

1426 MeV in  $K^{\text{bar}}N$ , 988 MeV in  $K^{\text{bar}}K$

$(K\bar{K}N)$  same result

Martinez Torres, Khemchandani, Oset, **PRC79**, 065207 (2009)

Martinez Torres, DJ, **PRC82**, 038202 (2010)

also found in calculation with fixed centre approximation

Xie, Torres, Oset, arXiv:1010.6164

**This state is essentially described by  $KK^{\text{bar}}N$  single channel in three-body configuration**

# Structure of $N^*(1910)$

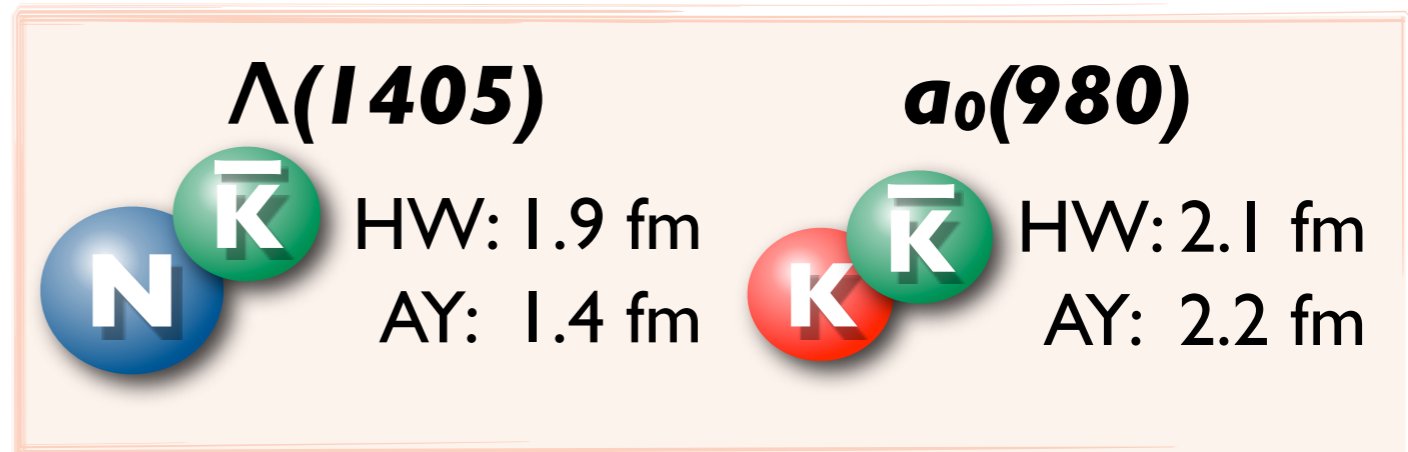
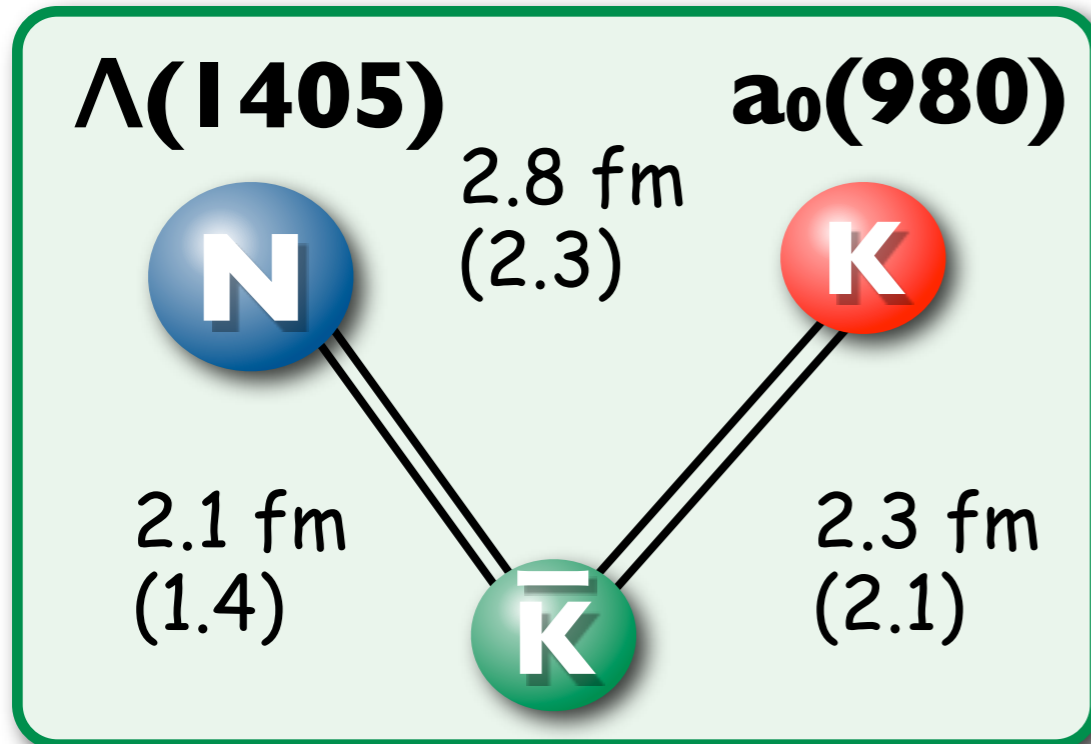
DJ, Y. Kanada-En'yo, PRC78, 035203 (2008)

## 1) relativistic potential model spatial structure

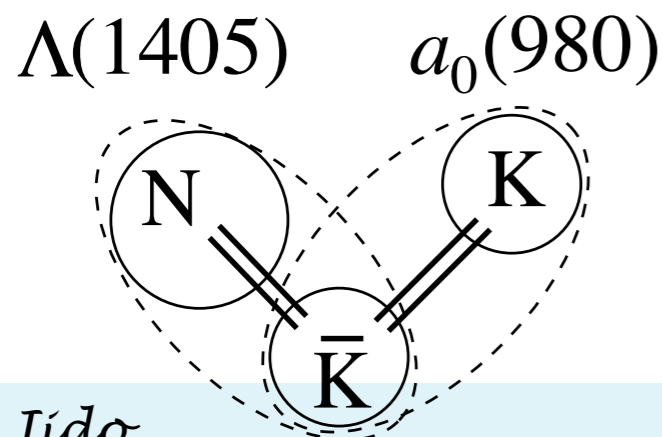
r.m.s radius: **1.7 fm** cf. 1.4 fm for  ${}^4\text{He}$

hadron-hadron distances are comparable  
with nucleon-nucleon distances in nuclei

mean hadron density: **0.07 hadrons/fm<sup>3</sup>**



- **coexistence of two quasi-bound states keeping their characters**



$\Lambda(1405) + K$

$a_0(980) + N$

- **main decay modes**

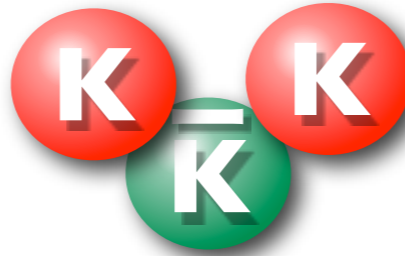
$\pi \Sigma K$  from  $\Lambda(1405)$

$\pi \eta N$  from  $a_0(980)$

# $K^{\text{bar}}KK$ system

## Kaon Ball

$K^*$   
 $J^P=0^-$



A. Martinez Torres, DJ, Y. Kanada-En'yo,  
arXiv:1102.1505 [nucl-th]

threshold: 1488 MeV

potential model

**1467 MeV (BE: 21 MeV), width 110 MeV**

Faddeev

**1420 MeV, width ~50 MeV**

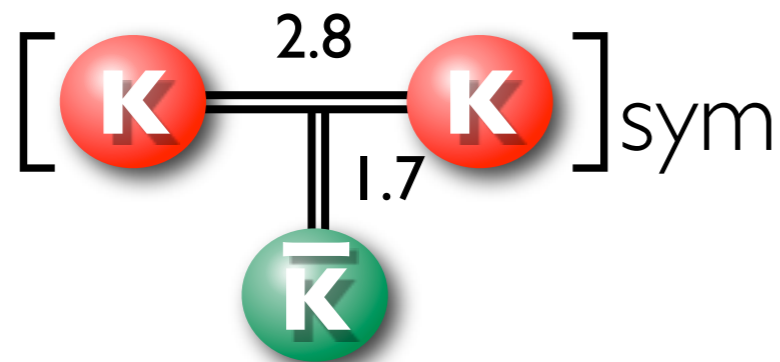
**$K^{\text{bar}}K$  Inv.Mass : 983 MeV ( $I=0$ ), 950 MeV ( $I=1$ )**

**spatial structure** obtained in potential model

r.m.s radius: **1.6 fm**

K-K distance: **2.8 fm**

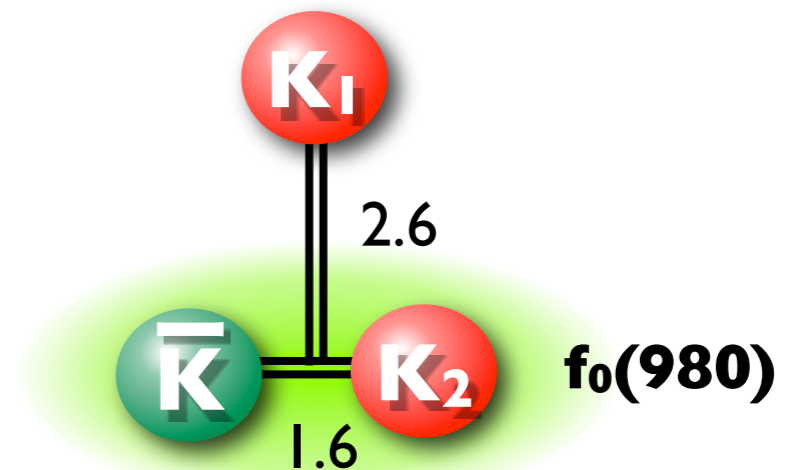
(KK)- $K^{\text{bar}}$  distance: **1.7 fm**



before symetrization ...

$K_2$ - $K^{\text{bar}}$  distance: **1.6 fm**

$K_1$ -( $K_2K^{\text{bar}}$ ) distance: **2.6 fm**

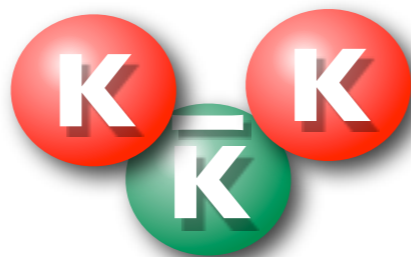


role of repulsive KK interaction

# $K^{\text{bar}}K$ system

## Kaon Ball

$K^*$   
 $J^P=0^-$



A. Martinez Torres, DJ, Y. Kanada-En'yo,  
arXiv:1102.1505 [nucl-th]

threshold: 1488 MeV

potential model

**1467 MeV (BE: 21 MeV), width 110 MeV**

Faddeev

**1420 MeV, width ~50 MeV**

**$K^{\text{bar}}K$  Inv.Mass : 983 MeV ( $I=0$ ), 950 MeV ( $I=1$ )**

- also found in  $f_0(980)K$ ,  $a_0(980)K$  two-body systems

Albaladejo, Oller, Roca, PRD82, 094019 (2010)

## PDG

**$K(1460)$**

$I(J^P) = \frac{1}{2}(0^-)$

OMITTED FROM SUMMARY TABLE

Observed in  $K\pi\pi$  partial-wave analysis.

$K(1460)$  seen in  $K\pi\pi\pi$   
partial wave analyses

omitted from summary table

large width

### $K(1460)$ MASS

VALUE (MeV)	DOCUMENT ID	TECN	CHG	COMMENT
• • • We do not use the following data for averages, fits, limits, etc. • • •				
~ 1460	DAUM	81C	CNTR -	63 $K^- p \rightarrow K^- 2\pi p$
~ 1400	<sup>1</sup> BRANDENB...	76B	ASPK ±	13 $K^\pm p \rightarrow K^\pm 2\pi p$
<sup>1</sup> Coupled mainly to $K f_0(1370)$ . Decay into $K^*(892)\pi$ seen.				

### $K(1460)$ WIDTH

VALUE (MeV)	DOCUMENT ID	TECN	CHG	COMMENT
• • • We do not use the following data for averages, fits, limits, etc. • • •				
~ 260	DAUM	81C	CNTR -	63 $K^- p \rightarrow K^- 2\pi p$
~ 250	<sup>2</sup> BRANDENB...	76B	ASPK ±	13 $K^\pm p \rightarrow K^\pm 2\pi p$
<sup>2</sup> Coupled mainly to $K f_0(1370)$ . Decay into $K^*(892)\pi$ seen.				

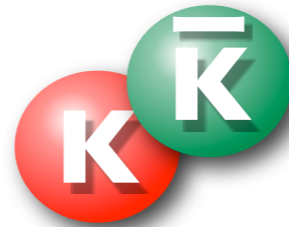
# Family of kaonic few-body nuclear systems

$\Lambda(1405)$



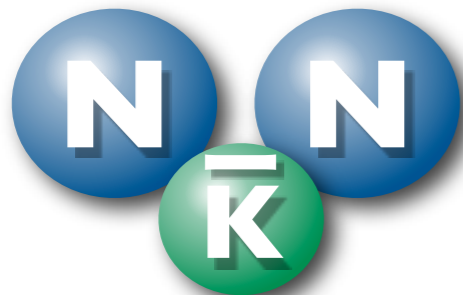
**BE ~10 MeV**  
(or more)

$f_0(980), a_0(980)$



**BE ~10 MeV**

$K^{\text{bar}}NN$



**BE ~20 MeV**  
(or more)

$N^*$

$J^P = 1/2^+$

$K^{\text{bar}}KN$

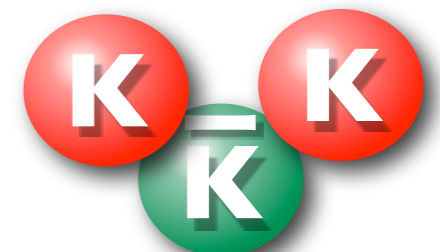


**BE ~20 MeV**

$K^*$

$J^P = 0^-$

$K^{\text{bar}}KK$



**BE 20~60 MeV**

$K^{\text{bar}}N$  and  $K^{\text{bar}}K$  interactions are “similar” in a sense of chiral dynamics

$\Lambda(1405)$   $f_0(980), a_0(980)$

**pion is too light to be bound in range of strong interaction**

# Exotic Hadrons from Heavy Ion Collision

Cho et al. (ExHIC collaboration), arXiv:1011.0852  
to be published in Phys. Rev. Lett.

## Basic ideas

- heavy ion collision as a factory of exotic hadrons
- extract hadron structure from production rates

**compact multi-quark system**

VS

**loosely bound hadronic molecular system**

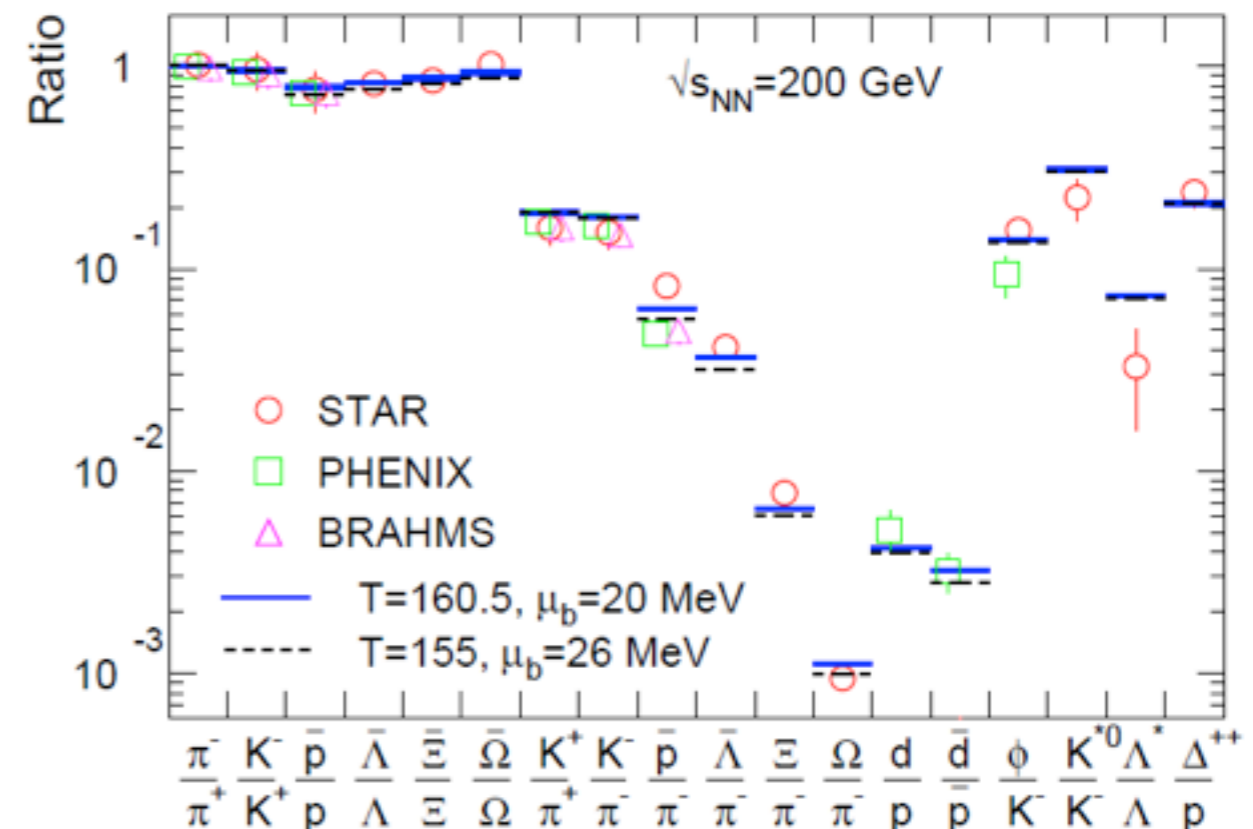
## Yield of Normal and Exotic Hadrons

### Statistical model

- ◆ Successful to describe yield of normal hadrons at RHIC
- ◆ Only sensitive to the mass (not quark content, size, ...)

### Coalescence model

- ◆ Successful to describe baryons &  $v_2$  at RHIC
- ◆ Sensitive to **quark content** and **hadron size**



*A. Andronic, P. Braun-Munzinger, J. Stachel,  
NPA772('06)167.*

# Hadron coalescence vs Quark coalescence

Cho et al. (ExHIC collaboration), arXiv:1011.0852  
to be published in Phys. Rev. Lett.

Coal./Stat. ratio:  $R_h = N^{\text{coal}}/N^{\text{stat}}$

Normal hadrons

→  $0.2 < R_h < 2$  (Normal band)

Multi-quark states

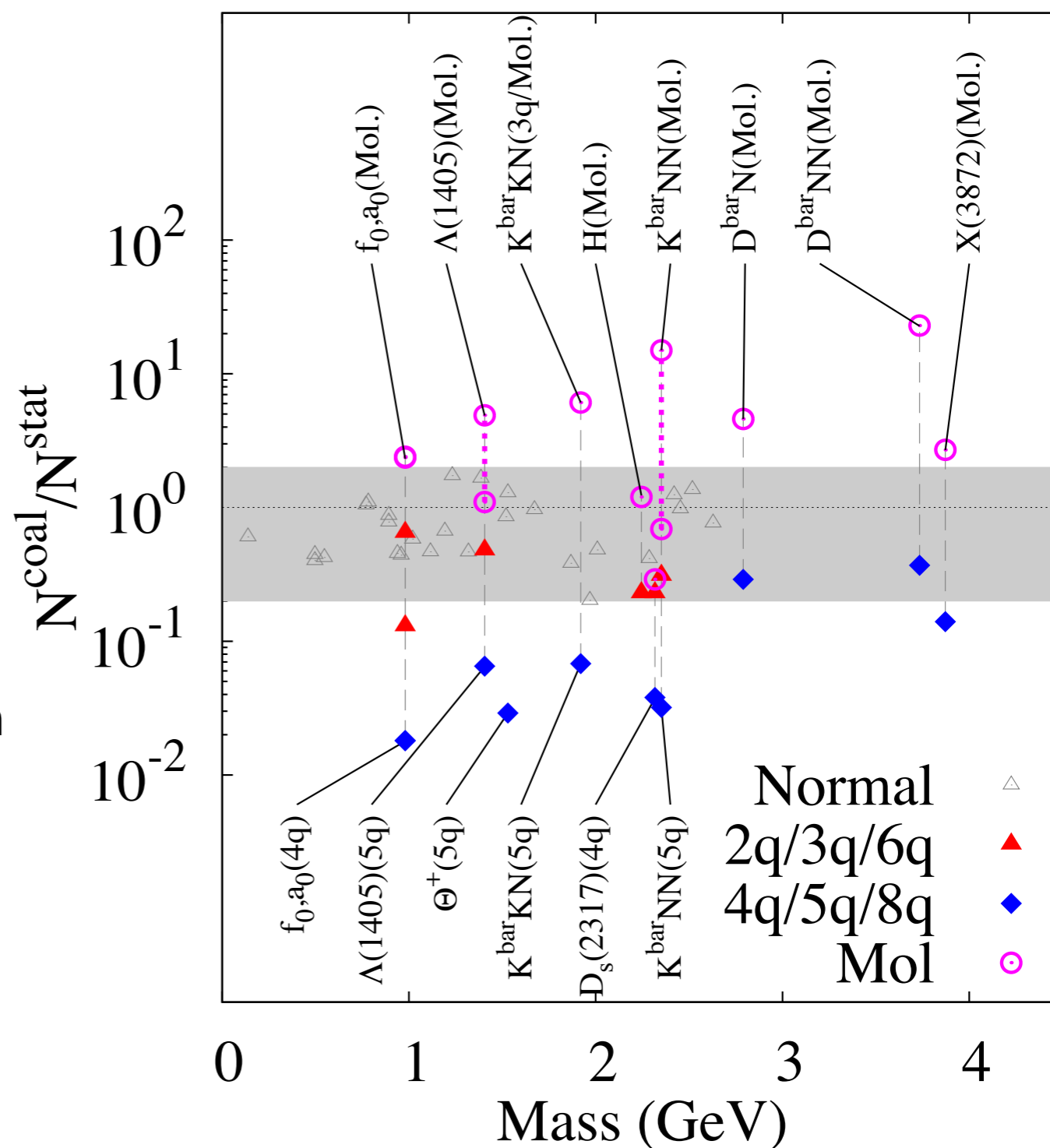
→  $R_h < 0.3$

Hadronic molecules

→ Large yields ( $R_h > 2$ )  
for weakly bound states

hadron coalescence after hadronization

Coal. / Stat. ratio at RHIC





# Summary

coupled channels approach (chiral unitary model) provides us with

**dynamical description** in meson-baryon scattering

describe both resonance and nonresonant scattering simultaneously  
applicable to reaction calculation

## **hadronic description**

all contents of the models are hadrons.

but, obtained hadron resonances are not necessarily hadronic composite objects.

source of quark dynamics can be hidden everywhere

(interaction terms, form factors, CDD poles,...)

thus, detailed theoretical analyses necessary to interpret the structure

## **microscopic description** in terms of hadrons

fundamental interactions are based on chiral effective theory

calculation of form factors

# Summary

## effective constituents in baryons structure

constituent quarks in low-lying baryons

hadrons can be effective constituents in some hadron resonances

## hadronic molecular states

hadron resonances composed by low-lying hadrons

self-bound systems

unique role of Kaon

new category of resonance

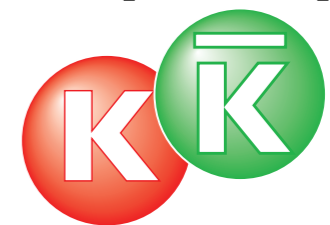
## heavy ion collision

factory of exotic hadrons  
production rates

$\Lambda(1405)$



$f_0(980), a_0(980)$



$K^{\text{bar}}KN$



$K^{\text{bar}}KK$



# Collaborators

## **origin (interpretation) of resonance pole**

T. Hyodo, A. Hosaka

Hyodo, DJ, Hosaka, PRC78, 025203 (08)

## **form factor of baryon resonance**

M. Döring, E. Oset

DJ, Döring, Oset, PRC77, 065207 (08)

T. Sekihara, T. Hyodo

Sekihara, Hyodo, DJ, PLB669, 133 (08);  
PRC83, 055202 (11)

## **kaonic few-body system**

Y. Kanada-En'yo, A.M. Torres

DJ, Y. Kanada-En'yo, PRC78, 035203 (08)

Martinez Torres, DJ, PRC82, 038202 (10)

A. Martinez Torres, DJ, Y. Kanada-En'yo,  
arXiv:1102.1505 [nucl-th]

# Kaonic few-body nuclear system

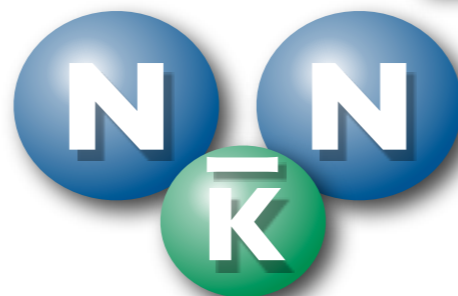
few body nuclear systems with one kaon

Nogami, PL7, 288 (1963)  
Akaishi, Yamazaki, PRC64,044005 (02)

$\Lambda(1405)$



$K^{\text{bar}}NN$



**BE: 10 or 30 MeV**

**single or coupled channel**

**achievement in theory : bound with a large width**

binding energies of  $K^{\text{bar}}NN$  system

## single channel

ATMS      Variational

Akaishi, Yamazaki

Dote, Hyodo,  
Weise

B.E. [MeV]

48

17-23

Width[MeV]

61

40-70

## coupled channel

Faddeev

Faddeev

Variational

Shevchenko, Gal,  
Mares

Ikeda, Sato

Wycech, Green

50-70

60-95

40-80

90-110

45-80

40-85

**issue is whether  $\pi\Sigma$  is active or not**